• **Write your name and UVa ID on the exam.** Pledge the exam before turning it in.

• There are 12 pages in this exam (including this one) and 7 questions, each with multiple parts. Some questions span multiple pages. All questions have some easy parts and some hard parts. If you get stuck on a question move on and come back to it later.

• You have 1 hour and 20 minutes to work on the exam.

• The exam is closed book, but you may refer to your two pages of notes.

• Even vaguely looking at a cellphone or similar device (e.g., tablet computer) during this exam is **cheating**.

• Please write your answers in the space provided on the exam, and clearly mark your solutions. You may use the backs of the exam pages as scratch paper. Please do not use any additional scratch paper.

• Solutions will be graded on correctness and clarity. Each problem has a relatively simple and straightforward solution. We might deduct points if your solution is far more complicated than necessary. Partial solutions will be graded for partial credit.

  
  – *Good Writing Example:* Python and Ruby have implemented some Smalltalk-inspired ideas with a more C-like syntax.

  – *Bad Writing Example:* Im in ur class, @cing ur t3stz!!

• If you leave a non-extra-credit portion of the exam blank, **you will receive one-third of the points for that portion (rounded down) for not wasting our time.** If you randomly guess and throw likely words at us, we will be much less sanguine.

  
  **UVa ID:** _________________________________

  **NAME (print):** _________________________________
### Problem Breakdown

<table>
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<th>Points</th>
</tr>
</thead>
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<td>1 — Type Checking</td>
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<td></td>
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<tr>
<td>2 — Operational Semantics</td>
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<td>3 — Code Generation</td>
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<td>4 — Analysis and Optimization</td>
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<td>5 — Linking, Loading</td>
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<td>Extra Credit</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td><strong>TOTAL</strong></td>
<td><strong>100</strong></td>
<td></td>
</tr>
</tbody>
</table>

**Honor Pledge:**

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How do you think you did? 

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1 Type Checking (16 points)

Consider an extension of Cool to support arrays of objects. We introduce an Array class that inherits from Object. Other classes cannot inherit from the Array class. We introduce four new expressions for manipulating Cool arrays:

\[
e ::= \text{new Array}[e] \\
\quad | \quad e_1[e_2] \\
\quad | \quad e_1[e_2] \leftarrow e_3 \\
\quad | \quad \text{foreach } v_i, v_e \text{ in } e_1 \text{ do } e_2
\]

Subexpressions are evaluated left-to-right (e.g., \(e_1\) before \(e_2\)). The first expression form creates a new array of size \(e\). The array initially holds \(e\) separate copies of \text{new Object}. The size must be non-negative at runtime to avoid an exception. The second expression form reads from array \(e_1\) at index \(e_2\), returning the object stored there. The third writes to array \(e_1\) at index \(e_2\) the value \(e_3\) (and returns \(e_3\)). For reads and writes, the index must be between 1 and the size of the array at runtime to avoid an exception. The final expression executes \(e_2\) for every element in array \(e_1\) with variable name \(v_i\) bound to the that element’s index and variable name \(v_e\) bound to that element’s value. Each element is considered in ascending order starting from 1. For example, this code:

```cool
let arr : Array <- new Array[3] in
arr[3] <- 5309;
arr[1] <- 867;
arr[2] <- "unicorn";
foreach i, elt in arr do {
  out_string("element "); out_int(i);
  out_string(" is ");
  case elt of
    n : Int => out_int(n);
    s : String => out_string(s);
  esac;
  out_string("\n");
}
```

Produces:

- element 1 is 867
- element 2 is unicorn
- element 3 is 5309

Give typing rules for the four new array expressions. Be as permissive as possible without permitting any unsafe programs. [4 pts] each.
\[ O, M, C \vdash \text{new Array}[e] : \]

\[ O, M, C \vdash e_1[e_2] : \]

\[ O, M, C \vdash e_1[e_2] \leftarrow e_3 : \]

\[ O, M, C \vdash \text{foreach } v_i, v_e \text{ in } e_1 \text{ do } e_2 \text{ done} : \]
2 Operational Semantics and Exceptions (24 points)

Following the previous problem, we extend our notion of Cool values $v$ to include array objects and a generic array exception used to report any array problem at run-time. Recall our use of a generalized return value $g$ to model exceptions.

$$
v ::= \text{void} \mid X(a_1 = l_1, \ldots, a_n = l_n) \mid \text{Array}(l_1, \ldots, l_n) \mid \text{ArrayException}
$$

$$
g ::= \text{Norm}(v) \mid \text{Exc}(v)
$$

Give the new operational semantics rules. Write only those rules where all subexpressions $e, e_1$ and $e_2$ return Normal values. [3 pts] each.

---

\[
\begin{align*}
\text{so}, E, S_1 &\vdash \text{new Array}[e] : \\
\text{so}, E, S_1 &\vdash e_1[e_2] : \\
\text{so}, E, S_1 &\vdash e_1[e_2] \leftarrow e_3 : \\
\text{so}, E, S_1 &\vdash \text{foreach } v_i, v_e \text{ in } e_1 \text{ do } e_2 :
\end{align*}
\]
3 Code Generation (12 points)

In this problem we consider code generation for the arrays introduced in the previous problems. Following the approach described in class, we decide to lay out array objects as follows:

<table>
<thead>
<tr>
<th>type tag</th>
</tr>
</thead>
<tbody>
<tr>
<td>object size</td>
</tr>
<tr>
<td>dispatch table pointer</td>
</tr>
<tr>
<td>array element 1 pointer</td>
</tr>
<tr>
<td>...</td>
</tr>
<tr>
<td>array element n pointer</td>
</tr>
</tbody>
</table>

[8 pts] Give the stack machine code generation rule for $cgen(e_1[e_2] \leftarrow e_3)$. You may assume there is a function at label `raise_ArrayException`; call to that label with no arguments to raise an `ArrayException` at run-time.

[4 pts] Give the general formula for $NT(e_1[e_2] \leftarrow e_3)$, the number of temporaries required.
4 Analysis and Optimization (15 points)

We desire to eliminate expensive array bounds checks at run-time in cases where we can prove statically that the indices are in bounds. To this end we introduce an internal analysis that tracks upper and lower bounds for integer variables. We write \([low, high]\) to indicate the bounds for a variable. The special values \(\infty\) and \(-\infty\) are also allowed in bounds. Thus, \([3, 3]\) means the variable is exactly 3, \([3, 5]\) means the variable must be between 3 and 5, and \([-\infty, \infty]\) means the variable could be anything. We also write \# for information at a location that is not (yet) reachable. For example:

```
arr <- new Array[10];
x <- 5;
if user_input() > 2:
x <- 3;
else:
x <- 7;
x <- x + 1;
arr[x] <- "alicorn";
```

At the end of the code snippet, \([4, 8]\) is a bound for \(x\), so we can eliminate the normal bounds check from the array write. We write \(B_{in}(x, s)\) and \(B_{out}(x, s)\) for the bounds values for \(x\) before and after statement \(s\), respectively. Give the local transfer functions for \(B_{out}\) in terms of \(B_{in}\). Assume \(B_{in}(x, s) = [a, b]\); do not consider \# for these four.

(a) [1 pt] \(B_{out}(x, x \leftarrow \text{const}) = \)

(b) [1 pt] \(B_{out}(x, y \leftarrow \ldots) = \)

(c) [2 pts] \(B_{out}(x, x \leftarrow x + \text{const}) = \)

(d) [1 pt] \(B_{out}(x, x \leftarrow \text{function}) = \)

(e) Fill in each blank with the most general and precise answer. [5 pts] each.
5 Linking, Loading and Libraries (10 points)

In the diagram below, two relocatable objects and their resulting linked executable are shown. The final addresses in the linked executable are shown underlined.

(a) [4 pts] Fill in each box labeled “Imports”, “Exports” or “Relocations” with the appropriate variable or label names.

(b) [6 pts] Label each offset measurement bar with the appropriate amount. Four of the bars are already labeled for you. Fill in the remaining five bars for Object A and three bars for Object B.
6 Game Theory (10 points)

Following our study of two-person impartial games of perfect information, we decide to extend Nim to be more forgiving. We consider a version of Nim in which you must remove one or more items from the same heap, but may also elect to take one item from a different heap if you like. (You don’t have to take that one extra item from a separate heap — you can skip that option.) We call this the “Nim With Interesting Takes” variant, or Nimwit.

Note that in Nimwit, two identical heaps need not be a loss for the current player. If you are facing two singleton heaps $A$ and $B$, you could take one from heap $A$ then elect to take one from heap $B$, leaving your opponent facing the empty board (and thus a game loss).

Consider the following Nimwit game of three heaps:

\[
\begin{array}{ccc}
A & A & \mid & B & \mid & C \\
\end{array}
\]

(a) [7 pts] If you are going first, what move would you make to win? Circle the items you would remove. (If you write in pen, think carefully first.)

(b) [3 pts] We mentioned in class that all impartial games are equivalent to Nim. What standard Nim sum does this Nimwit game equal? (That is, what height singleton standard Nim heap does it equal?)

7 Short Answer (18 points)

For each short answer question, limit your answer to at most four sentences.

(a) [3 pts] One weakness of the array approach considered here is that a case expression is typically required to make use of a retrieved object. Argue for or against the claim that a small change to SELF_TYPE could alleviate this problem.

(b) [3 pts] How would you change our array object layout to support inheriting from and extending the Array class?
(c) [3 pts] Argue for or against the claim that the debugging table approach described in class can be applied to programs that use stop-and-copy garbage collection.

(d) [3 pts] What information would need to be communicated by the compiler and/or runtime system to admit accurate sampling-based profiling in the presence of garbage collection?

(e) [3 pts] Suppose we are creating a Cool-to-C native interface. Fill in the source code below for a C method to convert Cool Int objects to C int values.

```c
int cool_Int_to_c_int(cool_object * cobj) {

}
```

(f) [3 pts] Suppose you are writing C code that is called from OCaml as part of a multi-language project. When would the runtime system ever need to invoke the garbage collector inside your C code?
8 Extra Credit (0 points)

“No Answer” is not valid on extra credit questions.

(a) [1 pt] Answer the following true-false questions about SELF_TYPE.

i. Circle true or false: $T \leq \text{SELF\_TYPE}_T$

ii. Circle true or false: SELF_TYPE helps us to reject incorrect programs that are not rejected by the normal type system.

iii. Circle true or false: SELF_TYPE is a dynamic type.

iv. Circle true or false: A formal parameter to a method can have type SELF_TYPE.

v. Circle true or false: If the return type of method $f$ is SELF_TYPE then the static type of $e_0.f(e_1, \ldots, e_n)$ is the static type of $e_0$.

(b) [1 pt] List one thing you would like to see changed or improved in the class. List one thing that you are enjoying.

(c) [2 pts] Cultural literacy. Below are the English translations or names for ten concepts or figures in world folklore, legend, religion or mythology. Each concept is associated with one of the ten most common languages (by current number of native-language speakers; Ethnologue estimate). For each concept, give the associated language. Be specific.

• _______________. The Pied Piper.
• _______________. The Eight Immortals.
• _______________. King Arthur.
• _______________. Kami.
• _______________. Kamayani.
• _______________. Jinn.
• _______________. Ilya Muromets.
• _______________. Endovelicus.
• _______________. Don Juan.
• _______________. Bankubabur Bandhu.
9 Twtr: Which tongues work best for microblogs? (0 points)

(for fun and stress relief only — no questions on this page)

The Economist – March 31st 2012

This 78-character tweet in English would be only 24 characters long in Chinese. That makes Chinese ideal for micro-blogs, which typically restrict messages to 140 symbols. Though Twitter, with 140m active users the world’s best-known microblogging service, is blocked in China, Sina Weibo, a local variant, has over 250m users. Chinese is so succinct that most messages never reach that limit, says Shuo Tang, who studies social media at the University of Indiana.

Japanese is concise too: fans of haiku, poems in 17 syllables, can tweet them readily. Though Korean and Arabic require a little more space, tweeters routinely omit syllables in Korean words; written Arabic routinely omits vowels anyway. Arabic tweets mushroomed last year, though thanks to the uprisings across the Middle East rather than any linguistic features. It is now the eighth most-used language on Twitter with over 2m public tweets every day, according to Semiocast, a Paris-based company that analyses social-media trends.

Romance tongues, among others, generally tend to be more verbose (see chart). So Spanish and Portuguese, the two most frequent European languages in the Twitterverse after English, have tricks to reduce the number of characters. Brazilians use “abs” for abraços (hugs) and “bjs” for beijos (kisses); Spanish speakers need never use personal pronouns (“I go” is denoted by the verb alone: voy). But informal English is even handier. It allows personal pronouns to be dropped, has no fiddly accents and enjoys a well developed culture of abbreviation. “English is unmatched in its acronyms, such as DoD for department of defence,” says Mohammed al-Basha, a spokesman for the Yemeni government, who tweets in English and Arabic.

Twitter’s growth around the world has reduced the proportion of total global tweets in English to 39% from two-thirds in 2009, but polyglot tweeters still often favour the language because of its ubiquity. Many Arabic-speaking revolutionaries used it to get their messages to a larger audience during the Arab spring, sometimes using automatic translation services. Until a recent upgrade, users of Arabic, Farsi and Urdu had trouble using hashtags (words prefixed with the # sign to mark a tweet’s subject). Some people use English to avoid censorship. Micro-bloggers on Sina Weibo (where messages containing some characters are automatically blocked) wrote “Bo” in English in order to comment freely about Bo Xilai, a purged party chief.

Though ubiquity and flexibility may give English hegemony, Twitter is also helping smaller and struggling languages. Basque- and Gaelic-speakers tweet to connect with other far-flung speakers. Kevin Scannell, a professor at St Louis University, Missouri, has found 500 languages in use on Twitter and has set up a website to track them. Gamilaraay, an indigenous Australian language, is thought to have only three living speakers. One of them is tweeting—handy for revivalists.